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# A RELIEFF attribute weighting and X-means clustering methodology for top-down product family optimization<sup>1</sup>

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This article proposes a top-down product family design methodology that enables product design engineers to identify the optimal number of product architectures directly from the customer preference data set by employing data mining attribute weighting and clustering techniques. The methodology also presents an efficient component sharing strategy to aid in product family commonality decisions. Two key data mining models are presented in this work to help guide the product design process: (1) RELIEFF attribute weighting technique that identifies and ranks product attributes, and (2) the X-means clustering approach that autonomously identifies the optimal number of candidate products. Product family commonality decisions are guided by once again employing the X-means clustering technique, this time to identify the components across product families that are most similar. A family of prototype aerodynamic air particle separators is used to evaluate the efficiency and validity of the proposed product family design methodology.

Keywords: data mining; X-means clustering; RELIEFF; bi-level quasi-separable problem; product architecture; aerodynamic particle separator

#### Nomenclature

- AF Air flow area.
- $f_k$  Local product design objective function(s), a function of local design variables:  $f_k(\mathbf{x}_k)$ .
- $\mathbf{R}^{Eng}$  Engineering design response (feasible/infeasible).
- $\mathbf{T}^{Cj}$  Vector of product attributes represented by the cluster centroid in the data mining model.
- $\mathbf{y}_{s,k}$  Linking variable at the engineering subsystem level cascaded up to system level.
- $\varepsilon_v$  Deviation tolerance between linking variables.
- $\xi$  Particle separation efficiency.
- $\mathbf{w}'$  The vector of newly transformed RELIEFF weights for target vector  $\mathbf{T}^{Cj}$ .
- $\|\cdot\|_2^2$  Squared L-2 norm notation measuring the deviation between targets and responses.
- *k k*th candidate product architecture determined by the results of the X-means clustering.
- K The total number of cluster centroids  $C_j$  that exist for the X-means clustering solution.
- $\frac{44}{45} \qquad Cost_k \qquad \text{Total product cost represented as the summation of individual component costs.}$

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#### 1. Introduction

53 In complex engineering systems that require a wide range of operating conditions, engineers 54 are left with the challenge of designing product portfolios that meet customer preferences. The 55 product family paradigm has been proposed to address the challenges of designing products 56 for mass customization or for highly diversified customer functionality requirements. The term 57 'product family' is frequently defined in literature as a group of related products that share an 58 underlying product design architecture (Messac et al. 2002, Alizon et al. 2007, Tucker and Kim 59 2007). The product family paradigm enables companies to standardize certain aspects of a product 60 and at the same time provide product diversity to customers through product variants. Product 61 cost savings may be realized as a result of product standardization due to 'economies of scale' 62 (e.g. cost sayings due to a standard manufacturing line for all products, rather than a specialized 63 manufacturing line for each product). However, greater product standardization may also lead 64 to lower product diversity in the market space and diminished product performance (e.g. limited 65 customizable features for customers such as product colour, reliability, size, etc.) Therefore, in 66 the product family approach, the level of product standardization versus product variety presents 67 a trade-off scenario as product performance and appeal (from the customer's perspective) may 68 diminish in an attempt to increase product standardization (Messac et al. 2002).

69 The product family design problem has been segmented into two well established domains: 70 the 'Bottom-Up' approach and the 'Top-Down' approach (Alizon et al. 2007). In the 'Bottom-71 Up' approach, companies are more interested in making significant improvements to an existing 72 product portfolio by combining products within the existing product family into a new product 73 architecture. An assumption in the 'Bottom-Up' approach is that the newly redesigned product 74 family will be able to satisfy customer needs through minimal additional technology investments. 75 On the other hand, in the 'Top-Down' approach to product family design, the next generation of 76 products is not based on an existing product family, but instead emerges from a market driven need. 77 This need arises from the evolution of customer preferences far beyond what the current product 78 portfolio can satisfy (Alizon et al. 2007). In this work, a 'Top-Down' product family methodology 79 is proposed that analyses large customer preference data sets and identifies candidate product 80 architectures that will be used in the product family design. This product design architecture can 81 represent a group of design components that perform a series of functional processes. Products 82 sharing similar product architecture can satisfy a broader range of customer requirements simply 83 by possessing functionality capabilities that vary beyond the underlying architecture. The sharing 84 of components also has the potential to reduce the time and costs associated with manufacturing 85 diverse products. The challenge of developing a product architecture to be used in a product family 86 presents an interesting design problem as the customer pool and functionality demands increase.

87 As data storage and information retrieval capabilities become more widely available, there is 88 an emerging trend for companies to acquire and store customer preference data. For example, 89 the physical characteristics (vehicle horsepower, number of doors, colour, etc.) of an automobile 90 purchased by a customer visiting a dealership, along with the customer's demographic information 91 (age, gender, household income, etc.) can enable auto manufacturers to determine emerging trends 92 in the automotive industry and design next generation products accordingly. A great challenge in 93 storing such data for product design purposes, however, is the non-homogeneity of customers, 94 along with their individual preferences. Therefore, as the size of this non-homogeneous data 95 increases, so does the complexity of identifying natural patterns within the data set. The ability 96 to determine suitable product architectures for a particular group of customers becomes a chal-97 lenge as enterprise decision makers and engineers attempt to extract meaningful patterns within 98 the data set to aid in the product design and development process. Data mining in the context 99 of product development is an emerging area of research that has the potential to significantly 100 impact engineering design and manufacturing efforts (Kusiak 2006, Tucker and Kim 2007). By

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identifying patterns within the large data set of customer preferences, engineers can incorporatethis knowledge in the product family design process.

103 The product family design scenario that this article focuses on is described as follows. An 104 enterprise is launching a portfolio of products that potentially share a subset of components. However, there are a few issues that must be resolved *prior to* the design process. First, the data 105 106 set used in this product portfolio design scenario comprises large-scale non-homogeneous data 107 which indicates that the product (the aerodynamic particle separator) undergoes a wide range of operating/environmental conditions. Second, the enterprise does not have a prior knowledge as 108 109 to how many product variants should be introduced in the market, although customer preference data is available from survey or market research. Third, the enterprise does not know which 110 components should be shared in case more than one product variant is introduced, although it has 111 112 the flexibility to accommodate the component sharing decisions.

113 This article presents a product family design methodology that is driven by data mining capabilities, which resolves the product family design challenges presented above. Often in the engineering 114 design process, quantifying attribute importance from a customer's perspective is challenging. 115 Possessing a mechanism that can identify which performance attributes are more dominantly 116 117 represented in the preference data set would help the engineering design teams focus resources 118 in a more efficient manner. For this, the RELIEFF (Kira and Rendell 1992) attribute weighting algorithm is employed to identify attributes in order of importance in the data set. Then, the X-119 means clustering algorithm is employed to identify groups of similar operating states within the 120 raw data set. As a result, the number of product variants that should be introduced to reflect prefer-121 122 ences (represented in the data) can be identified. Finally, the X-means clustering is applied again 123 to the detailed designs of the initial product variants to identify which components may be shared 124 among them. These sharing design decisions are implemented in a multi-disciplinary design optimization framework where an individual product variant is modelled as an individual subsystem. 125 The rest of the article is organized as follows. Section 2 provides research background followed 126 127

by the proposed methodology in Section 3; the methodology is demonstrated in a case study inSection 4 followed by results and discussion in Section 5 and conclusion in Section 6.

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#### 2. Research background

A selective literature review on research areas pertaining to the concepts and techniques proposed in this work will be presented. These research areas were reviewed in a selective manner based on their relevance to data mining in product family design/product portfolio optimization.

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# 138139**2.1.** Data mining in product design

140 There have been several researchers in the product design community that have incorporated data 141 mining techniques in the product design process. For example, Agard and Kusiak (2004) utilize 142 data mining clustering techniques to address the customer segmentation problem by determining 143 a target market in a new product development process. Association rule mining is then used to 144 discover attribute patterns in the segmented data (Agard and Kusiak 2004). Later works by Kusiak 145 illustrate the benefits of data mining in a wide array of diversified industries such as biotechnology, 146 energy, pharmaceutical, etc. (Kusiak 2006).

Tucker and Kim have incorporated data mining techniques in the product portfolio formulation process for extremely volatile markets (Tucker and Kim 2007, 2008). In such industries, product life cycles are short lived. Therefore, being able to correctly predict a customer's product preferences is paramount to increasing a product portfolio's chances of market success. Tucker and 151 Kim (2007) approached this design problem by systematically linking a customer's preferences, 152 acquired through predictive data mining techniques, directly with engineering detailed design 153 through multilevel optimization techniques (Kim *et al.* 2002, Kim *et al.* 2003).

Data mining techniques are also employed by Moon *et al.* (2006) in representing the functional requirements of customers. The proposed methodology uses fuzzy clustering techniques to determine the module composition of a product architecture (Moon *et al.* 2006). The work assumes that a product is an amalgam of module-based components with prior knowledge of the functionality capabilities of each module.

159 The primary contribution of this work is to present a product family design methodology for 160 complex engineering systems that autonomously identifies the number of products to design by extracting weighted product preference information from a customer data set. This work focuses 161 162 on design problems with large product preference data sets that can be integrated into the product design process. Since it would be impractical and highly expensive (from a cost and logistics 163 standpoint) to design an independent system for each operating scenario, the proposed methodol-164 165 ogy instead identifies the most similar operating requirements given a large data set of operating conditions/scenarios. This in turn highlights the cost savings associated with product platform 166 167 design through the concept of component sharing. This is modelled by the shared linking variable in the bi-level quasi-separable problem formulation that attempts to achieve an optimal design 168 solution for each product while concurrently satisfying specific product functionality requirements 169 170 (Tosserams et al. 2007). The term 'quasi-separable' is used in this work to denote independent sub-problems that share a common design variable/component. In this work, sub-problem simply 171 172 means a unique product design. The bi-level formulation is used in this work to co-ordinate these sharing decisions among sub-problems. Therefore, the individual sub-problem formulation for 173 174 the bi-level quasi-separable problem is as follows:

175 Minimize 176

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$$f_k(\mathbf{y}_{s,k}, \mathbf{x}_k) \tag{1}$$

Subject to:

$$g_k(\mathbf{y}_{s,k}, \mathbf{x}_k) \le 0 \tag{2}$$

$$h_k(\mathbf{y}_{s,k}, \mathbf{x}_k) = 0 \tag{3}$$

For the quasi-separable formulation, each  $\mathbf{x}_k$  represents the vector of local design variables unique to each sub-problem (*k*), where k = 1, ..., K sub-problems. The vector of linking variables  $\mathbf{y}_{s,k}$ makes the sub-problems quasi-separable as each sub-problem sharing a linking variable becomes influenced by the solution of other sub-problems sharing the same linking variable. A master problem is used to co-ordinate the linking variable among sub-problems and is explained in more detail in Section 3.2 of this work.

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#### 2.2. Product family optimization

192 The product family design paradigm has been investigated extensively throughout the engineer-193 ing design community. Although there are a wide range of application areas, the underlying 194 focus of product family optimization is to design a group of related products built around a common functional system architecture/platform. The aim is that commonality among prod-195 196 uct variants will reduce product design and manufacturing costs while still satisfying customer 197 requirements. There have been many proposed methodologies and metrics for evaluating product 198 commonality decisions in product family optimization. For example, the degree of commonal-199 ity index (DCI) proposed by Collier (1981) measures the ratio of common components existing 200 among products within a product family to the total number of components (Collier 1981). Later proposed commonality strategies such as the total constant commonality index (TCCI) (Wacker

201 and Trelevan 1986), the commonality index (CI) (Martin and Ishii 1996, 1997, Khajavirad and Michalek 2007), component part commonality index  $(CI^{(C)})$  (Jiao and Tseng 2000), product line 202 commonality index (PCI) (Kota et al. 2000), the percent commonality index (%C) (Siddique et 203 al. 1998), the generational variety index (GVI) (Martin and Ishii 2002), the functional similarity 204 index (FSI) (McAdams et al. 1999, McAdams and Wood 2002), and the comprehensive metric 205 for commonality (CMC) (Thevenot and Simpson 2007), propose strategies to help improve prod-206 207 uct commonality decisions by either rewarding or penalizing component sharing decisions. The aforementioned commonality indices are referenced in this work to give the reader a glimpse at 208 209 the myriad of approaches available to address the issue of commonality in product design and 210 development and how the proposed approach differs from them.

211 Instead of employing traditional commonality indices such as those listed above, product com-212 monality decisions are investigated by employing the X-means clustering technique during the 213 product family optimization process to identify similar components among product designs, 214 hereby avoiding the need to exhaustively search all possible component sharing possibilities. In the aerodynamic particle separator problem that is investigated, the X-means clustering tech-215 nique is first used to identify similarities among unique operating requirements. These clusters 216 217 will form the basis of the individual product platform. For the aerodynamic particle separator 218 problem, commonality decisions will be based primarily on the manufacturing costs associated 219 with each unique design. The costs savings benefits of incorporating commonality decisions in the product family design process will be presented later in this work. 220 221

#### 3. Methodology

225 Figure 1 is a flow diagram visually illustrating the sequence of the proposed product family design 226 methodology. Figure 1 begins with the acquisition of raw customer product preference data and 227 employs data mining attribute weighting and clustering techniques to determine the number of 228 unique products needed for a given data set. One of the novel contributions proposed in this 229 work, to solve the top-down product family research problem, is the ability to identify the optimal 230 number of product architectures based solely on the data set. For products with highly diverse 231 operating conditions, the data set itself may be highly heterogeneous making it quite difficult for 232 engineers to determine the number of products to design in order to satisfy the market space. By 233 employing the data mining RELIEFF attribute weighting and X-means clustering techniques to 234 the raw data set (Figure 1), engineers can determine the initial product architectures to design. 235

Steps 2 and 3 in Figure 1 illustrate the added benefits of component sharing by clustering similar products together in an attempt to reduce product design costs. The X-means clustering technique is employed at the engineering design level to determine which products are similar enough to potentially benefit from component sharing decisions. The details of Figure 1 will now be explained in depth in the following sections.

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#### 3.1. Data mining product preferences

The data mining of product preferences is the stage where dominant patterns are identified within the raw data set (Fayyad *et al.* 1996). With each unique instance in the data set representing a customer's preferred operating state for the product, the number of operating states can increase rapidly, thereby making it impractical for a single design to exist for each unique state. The engineering design goal is to identify those operating states within the data set that are similar in design requirements (as determined by the data mining algorithm). Since product attributes may vary in terms of design significance, an appropriate attribute weighting technique would help guide the engineering design process. To accomplish these product design challenges, the RELIEFF

C.S. Tucker et al.



Figure 1. Flow diagram of proposed product family design methodology: From data mining product architecture identification to component sharing through X-means clustering.

284 attribute weighting algorithm is first employed to weight attributes in order of importance in 285 the data set (Kira and Rendell 1992). Then the X-means clustering algorithm is used to identify 286 groups of similar operating states within the raw data set (illustrated in the data mining flow 287 diagram in Figure 1 and visually represented on the left in Figure 2). The weighted attributes will 288 influence both the data clustering process as well as the engineering design model as more valued 289 product attributes will be given more weight in the overall product family design methodology. 290 The X-means clustering algorithm is employed again in the component sharing decisions during 291 the product family optimization stage as similar individual product designs are grouped together 292 by similarity of design (Steps 2 and 3 in Figure 1 and visually represented on the right in Figure 2). 293 Below is an introduction to the RELIEFF attribute weighting technique that will later be applied 294 to the raw data set. 295

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### 3.1.1. RELIEFF product attribute weighting algorithm

In this work, the enhanced version of the RELIEF algorithm called RELIEFF is employed (Kononenko 1994). RELIEFF extends the original RELIEF algorithm by enabling it to efficiently



Figure 2. Visual representation of family design based on data mining RELIEFF attribute weighting and X-means clustering for product centroid generation and X-means clustering for product family component sharing optimization.

handle multi-class variables and also missing values within the data set (Kononenko 1994). A class variable can be thought of as the response or predictor variable of interest. Examples of class variables in product design data sets may include efficiency, energy consumption, price, etc.

The original RELIEF algorithm proposed by Kira and Rendell (1992) is an attribute evaluation technique that will enable product development engineers extract the importance of individual product attributes within a raw data set without explicit user provided ranking information (Kira and Rendell 1992). This can prove to be a vital time saving strategy, especially for extremely large data sets containing many attributes. Identifying the order of attribute relevance within a data set can reduce the overall computational complexity and increase the efficiency of data mining algorithms (Kira and Rendell 1992, Kononenko 1994).

Given a raw data set *S*, *m* instances are selected to serve as the number of sampled instances where *p* denotes the total unique attributes within the sample set *m* (Kira and Rendell 1992). The overall objective of the RELIEF algorithm is to take a random sample, and using a nearest neighbour search, to identify an identical class variable, which is defined as a NEAREST HIT (*H*), and also a different class variable that is nearest to the sample, defined as a NEAREST MISS (*M*) (Kira and Rendell 1992). The iterative process of RELIEF estimates attribute weights  $W[A_i]$ based on their similarity to a given class, where  $A_i$ , represents a unique attribute within the data set. The general form of the algorithm can be represented as follows (Kira and Rendell 1992).

Given *m*, the desired number of sampled instances, and *p*, the number of attributes, 1. set all weights  $W[A_i]$ : = 0.0; 2. for j := 1 to *m* do begin; 3. randomly select an instance X; 4. find nearest hit H and nearest miss M; 5. for i := 1 to k do begin; 6.  $W[A_i] := W[A_i] - \operatorname{diff}(A_i; X; H)/m + \operatorname{diff}(A_i; X; M)/m;$ 7. end; 8. end;

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#### C.S. Tucker et al.

where the *diff* function above measures the difference between the attribute being evaluated  $A_i$ taken from the randomly selected instance X, and the value of that same attribute given the closest hit (H) or closest miss (M). For discrete attributes, if the value of the attribute ( $A_i$ ) of the randomly selected instance (X) matches that of the nearest hit (H) or nearest miss (M), then the *diff* value is 0 (meaning values are identical), otherwise (1) meaning they are different. For continuous attributes, the actual difference is used and then normalized on a scale of [0, 1].

By its design, the RELIEFF attribute weighting technique does not constrain the attributes to non-negative values. Therefore, the weights will first be normalized based on the mini-max normalization (Han and Kamber 2006). For a given vector of attribute weights  $[w_1, w_2, ..., w_p]$ , the weights are normalized using the following formulation:

For weight  $i = 1, \ldots, p$ 

$$w'_{i} = \frac{w_{i} - \min}{\max_{w} - \min_{w}} (new_{\max_{w}} - new_{\min_{w}}) + new_{\min_{w}}$$
(4)

Here,

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$369$ $w'_i$ The newly transformed weight (i) of attribute (i). $370$ $\min_w$ The minimum value in the vector of RELIEFF attribute weights. $\max_w$ The maximum value in the vector of RELIEFF attribute weights.	
370 min <sub>w</sub> The minimum value in the vector of RELIEFF attribute weights.	
max The maximum value in the vector of DEL IEEE attribute weights	
371 max <sub>w</sub> The maximum value in the vector of KELIEFF attribute weights.	
$new_max_w$ The maximum value of the new range.	
$new_{\rm min}_{w}$ The minimum value of the new range.	

The new vector of weights  $\mathbf{w}'$  determines the level of importance for each target vector ( $\mathbf{T}^{Cj}$ ) at the engineering design level.

The data set with the newly updated weighted attributes will be used to:

- Weight clusters generated by the X-means clustering approach (discussed in the following section).
- Serve as attribute target weights for the engineering product design model.

#### 3.1.2. X-means clustering

The X-means clustering algorithm in data mining is an enhancement of the k-means clustering algorithm (Pelleg and Moore 2000). Before investigating the X-means clustering algorithm and its significance in product family optimization, the k-means algorithm will be briefly described.

389 Given a raw data set of unique customer preferences (operating conditions), the k-means 390 algorithm attempts to partition the original data set into k subsets of the data, where k represents the number of unique subsets or in the appropriate data mining terminology, clusters (Hartigan 391 392 and Wong 1979, Jain and Dubes 1988). Each cluster contains a centroid, with data points of the 393 cluster associated with this centroid. It is important to note that the number of clusters in the 394 k-means algorithm is given a priori as a user defined input. In the context of product family 395 design, this would be analogous to the engineering design team specifying the number of product 396 platforms that the customer's product operating requirements must adhere to. Rather than design 397 teams making postulations about the raw data set, a more natural process would be for the inherent 398 patterns of the raw data set to help guide the product platform number (this is one of the contri-399 butions of the X-means data mining technique). Although there have been many enhancements 400 to the k-means since its conception (Arora et al. 1998, Kanungo et al. 2002, Tarpey 2007), the

401 basic underlying mathematical formulation can be represented as follows:

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 $f = \sum_{j=1}^{K} \sum_{x_i \in S_j} \|x_i - c_j\|^2$ (5)

- 405 406
- 407 Here,  $S_j$  is a cluster of data points.
- Here, S will be defined as all instances in the raw data set and, therefore,  $S_j$  would simply be a subset of this.
- 410  $c_j$  is the centroid of a cluster  $S_j$ .
- 411  $x_i$  is a data point existing within a cluster.
- $\frac{11}{412}$  K is the total number of clusters (specified a priori by the user).
- The iterative process of the k-means algorithm begins by initially selecting the desired number of clusters  $(S_j)$  and making an initial guess of the cluster centroid values  $(c_j)$  (Hartigan and Wong 1979). The next stage involves assigning a data point to the closest cluster centroid and centroid value (if necessary) by minimizing the error function in Equation (5) until negligible deviation occurs with each iteration.
- 417 occurs with each iteration.
   418 The X-means clustering algorithm aims to improve on three key areas of the k-means algorithm
   419 (Pelleg and Moore 2000).
- 420 (1) Eliminating the need for number of clusters to be known as *a priori*. (2) I will be a set of the left a be a
- (2) Improving the computational scalability.(2) End of the computational scalability.
- 422 (3) Enhancing the search criteria for updating cluster centroids.

424 The process by which X-means achieves these improvements is in part based on its selection 425 criterion to determine when to add or replace a specific cluster centroid with child centroids. Child 426 centroids originate from splitting the original solution of a k-means iteration and determining if 427 the child clusters more accurately represent the data points once belonging to the parent centroid 428 (Pelleg and Moore 2000). The posterior probabilities will be used to rank the models  $Pr[M_i|D]$ , 429 where D represents the given data set and  $M_i$  represents each model with a given cluster size 430 k. The Bayesian information criterion (BIC) is used by X-means to rank which model is a more 431 accurate representation of the original raw data set. Mathematically, the BIC is represented as 432 follows (Kass and Wasserman 1995, Pelleg and Moore 2000): 433

434 435

$$BIC(M_j) = l_j(D) + \frac{p_j}{2}\log R$$
(6)

436 437 Here,

- $l_{38}$   $l_j(D)$  is the log likelihood of the data taken at the maximum likelihood point.
- $\frac{130}{439}$  D represents the given data set.
- $p_j$  represents the number of parameters in  $M_j$ .
- R is the total number of data points of candidate centroids.
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# 443 3.1.3. *Relevance of X-means to engineering product architecture design*

Engineering design problems involving a wide range of operating states specified by customers, can benefit from X-means clustering by identifying appropriate product functionality criterion for developing a product architecture and subsequent product family. The X-means clustering technique eliminates the need to guess the number of product architectures needed for a particular customer pool by analytically generating the appropriate number of clusters (product architectures) with corresponding product functionality specifications. A user instead specifies a 451 broad range for the number of clusters and X-means will identify the optimal cluster, given the 452 natural patterns within the data set (Pelleg and Moore 2000). This will ensure that the result-453 ing product family will be a true representation of the data set for which the designs are made. 454 Figure 2 illustrates how the cluster centroids of the X-means data mining clustering approach 455 are integrated into the engineering design. The product centroids illustrated in Figure 2 rep-456 resent the individual vectors of attribute value solutions that best describe *similar* groups of 457 customers within the raw data. Each unique product centroid will form a vector of product preference targets used to guide the product architecture optimization process. The engineer-458 459 ing design illustrated in Figure 2 represents the design of individual products based on the 460 X-means cluster centroids where each product will have unique functionality characteristics that aim to satisfy the overall customer preference targets. Section 3.2.3 describes how product vari-461 462 ants are then designed based on underlying product architecture under the notion of component 463 sharing.

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#### **3.2.** Engineering design optimization of product family

# 467 3.2.1. *Step 1: Individual product design optimization*

The results from the data mining stage provide product design engineers with several vital pieces of information. First, the results from the X-means clustering represent the vector of product attributes that form the product design targets ( $\mathbf{T}^{Cj}$ ) around which a product architecture is designed (Step 1 in Figure 1). Product design targets can range anywhere from physical product dimension targets such as length or width to product performance targets such as efficiency or speed.

475 The second vital piece of information from the data mining stage is the relevance of each 476 attribute target to the customer as determined by the RELIEFF attribute weighting technique. 477 That is, for each attribute target vector ( $\mathbf{T}^{Cj}$ ), there will be an accompanying vector of attribute 478 target weights w'. The engineering product architecture optimization is comprised of the detailed 479 engineering design model and incorporates the results from the data mining stage that help guide 480 the product architecture design. Here, local design variables are used to model the physical 481 dimensions and performance objectives of the product architecture subject to engineering design 482 constraints. 483

The general mathematical model for the engineering product architecture optimization is as follows:

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 Anote: The deviation is measured by the squared L-2 norm, which will be used throughout the engineering optimization models presented in this work. For example:

$$\|\mathbf{x} - \mathbf{y}\|_2^2 = \sum_i (x_i - y_i)^2.$$

 $\mathbf{g}_k(\mathbf{x}_{k,i}) \leq \mathbf{0}$ 

For the *k*th product architecture, Minimize

492 Minim 493

$$F(x)_{Architecture_{(k)}} = f_k + \mathbf{w}' \left\| \mathbf{T}^{C_j} - \mathbf{R}_k^{Eng} \right\|_2^2$$
(7)

496 Subject to:

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$$\mathbf{h}_k(\mathbf{x}_{k,i}) = \mathbf{0}$$

501	Here,	
502		
503 504	$f_k$	Local product design objective function (s), a function of local design variables: $f_k(\mathbf{x}_k)$ .
505	Ter	Vector of product attributes represented by the cluster centroid in the data mining
506 507		model. That is, for cluster centroid $C_j = [A_1, A_2,, A_p]$ , target $1^{C_j}$ is set as $[A_1, A_2,, A_p]$ where $A_1, A_2,, A_p$ represent attribute values for a given centroid $C_j$ .
508	w′	The vector of newly transformed RELIEFF weights for target vector $\mathbf{T}^{C_J}$ .
509	$\mathbf{R}_{k}^{Eng}$	Vector of engineering responses based on the formulation of the engineering design model, $\mathbf{R}_{k}^{Eng}$ is a function of local design variables $\mathbf{x}_{k}$ and is represented by $\mathbf{R}_{k}^{Eng}$
510 511		$(\mathbf{x}_k)$ .
512	$\mathbf{g}_k$	Inequality design constraints bounding the product architecture model.
512	$\mathbf{h}_k$	Equality design constraints bounding the product architecture model.
515 514	Κ	The <i>k</i> th candidate product architecture determined by the results of the X-means clustering.
515 516	Κ	The total number of cluster centroids $C_j$ that exist for the X-means clustering solution.
517		
518	Note: It i	is important to note that although there may be K candidate product architectures to investigate, there may not
519	always b	e a feasible design solution for the kth product architecture as generated product preference requirements may
520	be too de	emanding, given the constraints of the engineering design model. That is, at optimality $k < K$ .

523

#### 3.2.2. Step 2: Component sharing through X-means clustering

If a feasible design solution exists after Step 1, X-means data mining clustering technique is once
again employed, this time to determine the most similar product architecture design solutions
within the product portfolio. While the first X-means clustering technique helped identify the
similar groups of attributes in the raw data, the X-means clustering employed in Step 2 will
help identify the similar groups of design variable values among the feasible product architecture
design solutions (Step 2 in Figure 1).

For a given vector of design variables  $(\mathbf{x}_k)$  of an optimal product architecture solution, (where the objective function  $F(\mathbf{x}_k)$  of product architecture (k) has been minimized given the external targets  $\mathbf{T}^{Cj}$  and the local objective(s)  $f_k(\mathbf{x}_k)$ ), the goal is to determine the similarity among product architecture variable solutions. The notion is that the closer the optimal design solutions are, for example [ $(\mathbf{x}_k)$  and ( $\mathbf{x}_{k+1}$ )], the more likely these product architectures may be able to share certain design components.

537

# 538 3.2.3. Step 3: Product family optimization with shared design components 539

540 The third and final step in the proposed product family design methodology aims to reduce the product portfolio cost by sharing certain components among product architectures, thereby 541 creating a family of products (Step 3 in Figure 1). Since the component sharing decision is 542 543 inherently a combinatorial problem, Step 2 of the design methodology eliminates the need to search 544 all possible component sharing combinations by guiding the component sharing decisions based on the optimal solution of each resulting product architecture. Once similar product architectures 545 546 have been identified by the X-means technique in Step 2, the component variables are identified and modelled as linking variables  $(y_{s,k})$  in the quasi-separable bi-level problem. The model in 547 548 Step 1 is adapted into a bi-level hierarchical optimization model where level 1 strictly handles 549 the coordination of the linking variables and level 2 still remains the product architecture design 550 level, but this time including the linking variable targets as part of the objective function. The

#### C.S. Tucker et al.

bi-level design problem is modelled based on the quasi-separable problem (Kim 2001, Kim et al. 2002, Kokkolaras et al. 2002, Allison et al. 2006). A bi-level model is presented which comprises the component sharing co-ordination model at the upper level and the individual product design model at the lower level. At the component sharing level, updated linking variable values are distributed among product variants in an iterative manner until a feasible solution is achieved that is common among all product variants. If a feasible design solution does not exist for a given sharing scenario (that is, linking variable value  $y_s$  does not converge to a solution shared by all products), the original product design solutions (without shared variables) from Step 1 are kept. 

#### 561 Upper level: Component sharing co-ordination

The upper level (component sharing co-ordination) handles the coordination of linking variables to each of the product variants. In an effort to minimize design costs, certain design intensive and costly product components are shared among the different product variants. Under the quasi-separable formulation, these are represented as the linking variables  $(\mathbf{y}_{s,k})$ . The sharing strategy is handled at the component sharing level wherein updated linking variable values from the lower level product architecture design are cascaded up to the component sharing level. Constraint Equation (9) is formulated as an inequality rather than an equality constraint due to numerical difficulties reported in the literature of equality constraint based bi-level formulations that fail to satisfy the standard Karush-Kuhn-Tucker (KKT) conditions for a constrained optimization problem (Alexandrov and Lewis 2002).

572 Minimize

Subject to:

$$g1: \sum_{k \in Q} \left\| \mathbf{y}_{s} - \mathbf{y}_{s,k}^{Eng} \right\|_{2}^{2} - \varepsilon_{\mathbf{y}} \le 0$$
<sup>(9)</sup>

(8)

Here,

ue.
be
ble(s)
ł

 $\varepsilon_{\mathbf{y}}$ 

 $\mathbf{y}_{s,k}^{Eng}$  Linking variable value at the lower level cascaded to the upper level. This is constant at each iteration in the above formulation that is subsequently updated at the engineering product architecture optimization level after each iteration.

*k* The *k*th candidate product architecture that has been identified for component sharing.

- *Q* The total number of products that exist in a particular candidate product family. This is based on the X-means cluster solutions described in Step 2. The term candidate product family is used because until a feasible design solution can be achieved for the shared component case, these *Q* products will remain unique products within the product portfolio (note that  $Q \le K$  which simply means that the number of candidate product families cannot exceed the total number of unique products that initially exist).
- $\begin{array}{c} 597 \\ 598 \\ 598 \\ 599 \\ 600 \end{array}$  Deviation tolerance between linking variables. For each shared variable, another constraint g(i) is added based on a similar formulation as equation (9) and add another tolerance variable in the objective function to represent this additional shared variable.

Lower level: Product family optimization

602 603	In the k	th sub-problem,
604	Minim	$  _{-C} = Eng  ^2   _{-U} =   _{-C}$
605 606		$F(x)_{Architecture_{(k)}} = f_k + \mathbf{w}' \left\  \mathbf{T}^{C_j} - \mathbf{R}_k^{\text{Ling}} \right\ _2 + \left\  \mathbf{y}_s^{C} - \mathbf{y}_{s,k} \right\ _2^2 $ (10)
607	Subject	t to:
608		$\sigma(\mathbf{x}, \mathbf{y}) < 0$
609		$\mathbf{g}_k(\mathbf{x}_k,\mathbf{y}_{s,k}) \leq 0$
610		$\mathbf{h}_k(\mathbf{x}_{k,} \mathbf{y}_{s,k}) = 0$
611	Here,	
612	£	I and any dust desire shireting function (s)
613	$J_k$ $\mathbf{T}^{C_j}$	Local product design objective function (s).
614 615	1	model. That is, for cluster centroid $C_i = [A_1, A_2, \dots, A_n]$ , target $\mathbf{T}^{C_j}$ is set as
616		$[A_1, A_2, \dots, A_n]$ where $A_1, A_2, \dots, A_n$ represent attribute values for a given
617		centroid $C_i$ .
618	$\mathbf{w}'$	The vector of newly transformed RELIEFF weights for target vector $\mathbf{T}^{Cj}$ .
619	$\mathbf{R}_{k}^{Eng}$	Vector of engineering responses based on local design variables. $\mathbf{R}_{k}^{Eng}$ is a function of
620	ĸ	local design variables $\mathbf{x}_{k}$ and is represented by $\mathbf{R}_{k}^{Eng}$ ( $\mathbf{x}_{k}$ , $\mathbf{y}_{s,k}$ ).
621	$\mathbf{g}_k$	Inequality design constraints.
622	$\mathbf{h}_k$	Equality design constraints.
623	$\mathbf{y}_{s}^{U}$	Linking variable target value cascaded down to the lower level from the upper level; a
624		constant value at each iteration that is subsequently updated with each successful
625		iteration.
626	$\mathbf{y}_{s,k}$	Linking variable at the lower level. This is local to the kth model and attempts to match the value of $\mathbf{x}^U$ at each iteration
628		the value of $\mathbf{y}_s$ at each iteration.
629	The	overall flow of the proposed product family optimization is succinctly described below:
630	Bi-leve	l product family optimization
631	Step 1	
632	Given	w' vector of weights and $\mathbf{T}^{C_j}$ targets, where length(w') = length( $\mathbf{T}^{C_j}$ ) and K cluster
633	centro	ids:
634	1. Se	blve K engineering design problems (with no linking variables $\mathbf{y}_{sk}$ ) weighting each
636	1	$\Gamma^{C_j} - \mathbf{R}_{\iota}^{Eng} \parallel_2^2$ based on RELIEFF;
637	2. If	solution exists for the Individual Product Design Optimization Model (i.e., optimal
638	1	$\mathbf{\Gamma}^{C_j} - \mathbf{R}_k^{Eng} \ _2^2$ solution while satisfying local objectives and constraints);
639	3. O	ptimal solution found for weights $\mathbf{w}'$ and targets $\mathbf{T}^{Cj}$ without sharing components;
640	Step 2	2:
641		· · · · · · · · · · · · · · · · · · ·
642	4. Ei	mploy <b>X-means</b> clustering to identify candidate product families based on solution
643	SI	milarities from Step 1;
644	Step 3	3:
645 646	5 50	alve hi-level quasi-separable problem (component sharing among products) using the
647	$\int J = \frac{1}{U}$	<i>pper Level-Lower Level</i> formulation with linking variables v <sub>e</sub> .
648	6 If	feasible solution exists (i.e., <i>ontimal</i> $\ \mathbf{T}^{C_j} - \mathbf{R}_{j}^{Eng}\ _{2}^{2}$ and $\ \mathbf{v} - \mathbf{v}^{L_j}\ _{2}^{2}$ at the Lower Level
649	ar	and also optimal $\varepsilon_v$ at the Upper Level, ( $\varepsilon_v$ should be close to 0 at the Upper Level, indicating
650	a	feasible shared component among product variants within a product family));

	14	C.S. Tucker et al.
651 652 653 654 655 656 657	<ol> <li>7. Op pro</li> <li>8. Els for</li> <li>9. end</li> <li>10. end</li> </ol>	timal solution found for weights $\mathbf{w}'$ and targets $\mathbf{T}^{Cj}$ and linking variables $\mathbf{y}_{s,k}$ for each duct variant; e, solution does not exist for linking variable scenario; that is, sharing $\mathbf{y}_{s,k}$ is not feasible product variants, therefore keep initial solutions found from <b>Step 1</b> ; l;
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#### 4. Application: Aerodynamic particle separator case study

Indoor air quality (IAQ) is becoming an increasing concern for human health. Particulate matter is a leading cause of human respiratory illness in addition to degrading the performance of heating ventilation and air conditioning (HVAC) systems (WHO). As a result, abatement technologies for these aerosols are in high demand. Aerodynamic particle separators are filter-less air cleaning devices that can be capable of removing micron size particles with low energy consumption and minimal maintenance (Zhang 2005). Determining the optimal aerodynamic particle separator design for a specific application is challenging when taking into account its unique system requirements and environmental conditions.

#### 4.1. The engineering design problem

#### 4.1.1. Aerodynamic particle separator design

To demonstrate the effectiveness of the proposed design methodology, the design of a uniflow type
particle separator is investigated (illustrated in Figure 3). The basic design of this device can be
partitioned into three sections: (1) vane section, (2) straight region and (3) converging region/dust
bunker. These sections are defined by eight design variables as shown in Figure 3 and Table 1.

679 The performance of an aerodynamic particle separator design is strongly dependent on system 680 requirements and environmental conditions. System requirements such as the air cleaning effi-681 ciency, pressure drop (thus power consumption), air flow rate and overall device size contribute 682 to the design objectives and directly define the constraints for a given application. Environmen-683 tal conditions, including the air properties and contaminant particle size distribution can have a 684 significant impact on the performance of a particular design and must also be incorporated into 685 the system model (Barker 2008). Together, these two groups can be used to characterize a given 686 application or operating state. These factors can vary by an order of magnitude between different applications, thereby complicating the design process. The product architecture design objective will, therefore, be to minimize cost while satisfying external product preference targets and local



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Figure 3. Uniflow type aerodynamic particle separator flow pattern and design variables.

Variable	Units	Description
$r_1$	Meters (m)	Inner tube radius
$r_2$	Meters (m)	Outer tube radius
$L_S$	Meters (m)	Maximum pressure drop
α	Radians (rad)	Vane discharge angle
$L_C$	Meters (m)	Length of converging gap
r <sub>3</sub>	Meters (m)	Radius of exit tube
$L_E$	Meters (m)	Length of exit tube
N	#	Number of units in paralle

 Table 1. Design variable notation for aerodynamic particle separator.

design constraints. The broader enterprise portfolio objective will be to minimize overall product
 design and development costs by capturing the component sharing opportunities that exists within
 the product portfolio.

#### 717 **4.2.** Data mining product preferences

#### 718 719 4.2.1. *Raw data set of product operating states*

A data set of 1000 operating states was generated to simulate the large variation in physical requirements and environmental conditions characterizing the broad range of applications in which aerodynamic particle separators are frequently employed (Barker 2008). Table 2 represents a snapshot of the 1000 operating states with distinct product attributes and environmental conditions represented by each column. Section 5 of the article presents the results from both the RELIEFF attribute ranking algorithm and the X-means data mining clustering approach and demonstrates how the data mining process influences product family design efforts.

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# 729 4.2.2. *RELIEFF attribute weighting* 730

The results from the RELIEFF attribute ranking approach in Table 3 reveal that the two engineering 731 design targets—efficiency ( $\zeta$ ) and flow area (AF<sub>max</sub>)—have normalized weights of 0.1687 and 732 0.0785 respectively. The other attributes in Table 3 are used as design parameters in the engineering 733 design model and, therefore, also play a significant role in the overall optimal solution. The 734 efficiency ( $\zeta$ ) and flow area ( $AF_{max}$ ) are selected based on the type of engineering problem being 735 solved (in other applications, one may choose to set all attributes in the data set as targets for the 736 product architecture design model). This vital information is a data pre-processing step that will 737 help generate product cluster centroids that take into account the weighted attribute preferences 738 of the different operating states given by the raw data set. 739

- *Note:* RELIEFF results were obtained using Weka version 3.5.8 (Witten and Frank 2005) and it took approximately 20
   seconds running on a Intel Pentium Duo 2.5 GHz Processor. The normalized attribute weights are based on Equation (4)
   in Section 3.1.1.
- 743

Table 2. Snapshot of aerodynamic particle separator data set consisting of 1000 states.

	Q (m3/s)	$\Delta_{P \max}$ (Pa)	L <sub>max</sub> (m)	$\begin{array}{c} A_{Fmax} \\ (m^2) \end{array}$	N <sub>max</sub> # units	F(d <sub>p</sub> ) (%)	$ ho_{p}$ (kg/m <sup>3</sup> )	<i>T</i> <sub>air</sub> (°C)	P <sub>air</sub> (kPa)	Efficiency %	Price \$
State 1	1.58	250	1	0.5	50	A1	2650	20	101	82	1,200
State 2	1.48	200	0.3	0.1	3	A4	2650	0	99	85	450
State 3	1.27	1500	1.5	1.5	16	Limestone	2700	500	200	90	900

Attribute Rank	Attribute Name	Attribute Weight	Normalized Attribute Weight
Highest	Nmax	0.0881	1.0000
Ĩ	Efficiency	0.0110	0.1687
	Tair	0.0100	0.1575
	Pair	0.0099	0.1570
	Q	0.0073	0.1287
	Dpmax	0.0036	0.0888
	Afmax	0.0026	0.0785
	Lmax	0.0018	0.0695
	Rhop	-0.0006	0.0433
$\downarrow$	Operating States	-0.0031	0.0169
Lowest	Fdp	-0.0046	0.0000

Table 3. Attribute ranking of raw dataset via RELIEFF algorithm.

#### 4.2.3. Data mining X-means clustering results

The X-means clustering results reveal that a total of five clusters most accurately represents the similarities in the data set of 1000 operating states. The results from Table 3 represent the product design targets and parameters for the product portfolio of aerodynamic particle separators. Initially, each product centroid will be used to design an individual aerodynamic particle separator. Component sharing benefits will then be presented based on the vane section component. [Results attained using Weka version 3.5.8 (Witten and Frank 2005) and Data to Knowledge D2K (McEntire 2003)].

#### 4.3. Engineering design optimization of product family

#### 4.3.1. Step 1: Individual product design optimization

The X-means clustering algorithm generates k = 1, ..., 5 clusters, each with unique centroids *C<sub>j</sub>*. Based on the results from the X-means clustering, and the RELIEFF attribute weights accompanying each cluster centroid, engineers can now determine whether an optimal product design solution exists based on the aerodynamic particle separator response model.

The aerodynamic particle separator objective function attempts to match the particle separation efficiency target  $(\zeta_k^{\hat{C_j}})$  and the flow area target  $(AF^{C_j})$  generated from the X-means clustering results while at the same time minimizing product design and manufacturing cost objective. The attributes within a cluster centroid ( $C_i$ ) will form the design/environmental parameters of the model. The efficiency model selected was initially developed by Zhang (2005) and later augmented by Barker (2008). In this model, the flow is assumed to be fully turbulent and the steady state particle motion results from a balance between the centrifugal force and aerodynamic drag in the Stokes regime (Zhang 2005). The vector  $\mathbf{x}$  contains the eight design variables as described by Table 1 and Figure 3. The cost function was based on the estimated mass of material required and injection moulding costs of the vane section. The material selected is an engineered polymer with a density of 1200 kg/m<sup>3</sup> at a cost of \$3.00 per kilogram. The injection moulding cost is estimated at a fixed cost of \$10,000 per design for the required capital equipment and labour. The efficiency model as a function of variables in x and particle size  $d_{p_i}$  is shown in Equation (11). The total efficiency for a given particle size distribution is then calculated by Equation (12). 

$$\xi(\mathbf{x}, d_{p_i}) = 1 - \exp\left(-\frac{\rho_p d_{p_i}^2 C_c Q \tan(\alpha) L_S}{9\eta(r_2^2 - r_1^2)}\right) \cdot \exp\left(\frac{\rho_p d_{p_i}^2 C_c (V_t^2 G_t(\mathbf{x}) + V_z^2 G_r(\mathbf{x}))}{\eta V_z}\right) \quad (11)$$

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$$\xi_T = \sum_{i=1}^N \xi(\mathbf{x}, d_{p_i}) \cdot F(d_{p_i})$$
(12)

804 Her

004	Here,		
805	Ca	Cunningham slip correction factor	
806		Diameter of particle (i) m	
807	$u_{p_i}$	Diameter of particle (1), in:	
808	$r(a_p)$	Finite size distribution.	
809	$G_t(x)$	Efficiency model geometric relationship between design variables, tangential	L
810	$C(\omega)$	acceleration.	
811	$G_r(x)$	Enciency model geometric relationship between design variables, radial accele	gration.
812	$ ho_p$	Particle density, kg/m <sup>3</sup> .	
813	η	Air viscosity, Pa·s or kg· m/s.	
814	$\underline{Q}$	Air flow rate, m <sup>3</sup> /s.	
815	$V_t$	Tangential velocity of particle mixture.	
816	$V_z$	Axial velocity of particle mixture.	
817	$r_1$	Inner tube radius.	
818	$r_2$	Inner tube radius.	
819	α	Vane discharge angle.	
820	$L_S$	Maximum pressure drop.	
821	The end	ineering design model for the perodynamic particle separator can be mathem	atically
822	renresen	intering design moder for the derodynamic particle separator can be mathem	attearry
823	kth aaro	dynamic narticle senarator	
824	Minimiz		
825	IVIIIIIIIIZ		
826		$F(x)_{i=1} = w' \  z_i^{C_j} - z_i^{Eng} \ ^2 + w'_{i=1} \  A F_i^{C_j} - A F_i^{Eng} \ ^2 + Cost_i$	(13)
827		$\  \langle w \rangle_{Architecture_{(k)}} - w \xi \  S_k - S_k \ _2 + w AF \  M k \ _2 + COST_k$	(15)
828	Subject	to:	
829	Pressure	e drop constraint (g1):	
830		$P_T(\mathbf{x}) - P_{\max} < 0$	(14)
831	-		()
832	Face are	a constraint (g2):	
833		$4r_2^2N - AF_{\max} \le 0$	(15)

834 Product length constraint (g3):835

$$L_V + L_S + L_C + L_E - L_{\max} \le 0$$
 (16)

837 838 Here,

- $AF_k$  Maximum allowable face area perpendicular to air flow direction.
- 840  $w'_{\zeta}$  Efficiency RELIEFF attribute weight.
- 841  $w'_{AF}$  Flow area (AF) RELIEFF attribute weight.
- 842  $L_{\text{max}}^{AF}$  Total allowable length of the system.
- $L_V$  Length of vane section.
- $L_s$  Length of straight region.
- $L_C$  Length of converging region.
- 846  $L_E$  Length of exit tube.
- 847  $P_T(\mathbf{x})$  Total pressure drop of the system as a function of design variables  $\mathbf{x}$ .
- 848 *N* Number of aerodynamic particle separator units in one module.
- 849  $P_{\text{max}}$  Maximum allowable pressure drop (air flow restriction).
- 850  $Cost_k$  Total product cost represented as the summation of individual component costs.

851 *Note:* The design model is also bounded by a set of linear inequality constraints  $Ax \le b$  and con-852 straints Equations (14)–(16) that can be further expanded. A more detailed design model can be found 853 in Barker (2008).

854 855

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#### 4.3.2. Step 2: Component sharing through X-means clustering

If an optimal solution exists for the aerodynamic product portfolio based on the X-means clustering
 targets, the next step is to determine whether additional costs savings can be realized by sharing the most design intensive components among different product architectures. The X-means
 clustering technique is employed to determine the similarities among the unique aerodynamic
 particle separator designs based on the solution results after Step 1. A successful sharing solution
 among products represents a unique product family. The results from the unique aerodynamic
 particle separator solutions can be seen in Table 5 which is further explained in Section 5.1.

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#### 4.3.3. Step 3: Product family optimization with shared design components

867 For the aerodynamic particle separator case study, the vane section is the most design intensive 868 and costly component. The complex curved vanes must be injection moulded, which requires a 869 unique mould to be machined for each vane section design. By employing the X-means clustering 870 technique, product engineers will be able to (1) determine which product architecture designs are 871 similar based on the solutions attained during Step 1 and (2) determine the number of candidate 872 product families to include in the enterprise product portfolio based on the number of X-means 873 cluster centroids generated. The L2 norm distance measure used by X-means will favour those 874 design solutions that are numerically close to one another. This will help guide the sharing decision 875 of the vane section as products with close numerical values for the variables that define the vane 876 section (vane angle  $\alpha$ , the inner and outer tube radii  $r_1$  and  $r_2$ ) will be favoured within a given 877 cluster centroid. 878

#### Upper level: Component sharing co-ordination

The upper level (component sharing co-ordination) of the aerodynamic particle separator model will handle the co-ordination of the shared vane section among product families. The component

Q19886 Table 4. Product cluster centroids based on X-means clustering algorithm.

		System requirements				System requirements					
States	Q (m3/s)	$\Delta_{P \max}$ (Pa)	L <sub>max</sub> (m)	$\begin{array}{c} A_{Fmax} \\ (m^2) \end{array}$	N <sub>max</sub> # units	F(d <sub>p</sub> ) (%)	$ ho_{p}$ (kg/m <sup>3</sup> )	<i>T</i> <sub>air</sub> (°C)	P <sub>air</sub> (kPa)	Efficiency %	Price \$
Produc 285	t Centroid 1 1.20	463	0.71	0.60	36	Limestone	2226	25	100	78	962
Produc 765	t Centroid 2 3.39	1507	0.79	0.68	39	A4	2211	71	111	86	1,168
Produc 750	t Centroid 3 3.36	1623	0.67	0.55	14	Limestone	2389	72	107	85	411
Produc 456	t Centroid 4 1.94	911	0.72	0.62	24	A1	2278	45	102	80	632
Produc 260	t Centroid 5 1.29	458	0.69	0.75	11	Limestone	2225	24	100	78	290

901 902		al	Cost	95.41	0.02 ct	9.65	42.41
903		Tot	s	5,55	4, 9, 4	4,15	3,74
904			Proc	0,	10	S	0
905				_		_	_
906		ion	Cost	0.00	20.0	00.0	0.0
907		ject	s	00,00	38	00,	,00
908		In	W	10	2 2	10	10
909		~					
910		nits	ster	26	73	33	61
911		С #	Clus (# t	00	- 1	0	-
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924			(m	0.0		<u>.</u>	o.
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926			AF leter	120	453(	49	1020
927			u)	0.0	0 0	ö	o.
928	÷		rs)	33	05	33	80
929	ign		r3 1ete	.116	02	.06	.106
930	. des		(n	0		0	0
931	ator	es	ers)	6	80 91	2	95
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936	ami		s)	~	~ ~		~
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938	aerc		(me	0.0	0 0	0.0	0.0
939	ual		s)	90		4	9
940	ivid		r2 eter	193	400 099	080	193
941	ind		(m	0.0		ö	0.
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948	S.		ct	le S.	le v V v	le S	le S
949	ble		npo	utic	uruc rtic	utic	urtic
950	Ta		Pr	$P_{a}$	Ъа	$P_{\hat{a}}$	$\tilde{P}_{\tilde{a}}$

Engineering Optimization

173,910.93

Total Product Portfolio cost

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951 sharing objective function will minimize the tolerance deviation variable of each shared variable. 952 There are three variables that define the vane section, including the vane angle  $\alpha$ , the inner and 953 outer tube radii  $r_1$  and  $r_2$ .

#### 954 **Minimize** 955

 $\varepsilon_{\alpha} + \varepsilon_{r_1} + \varepsilon_{r_2} \tag{17}$ 

957 Subject to:

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$g1: \left\  lpha_s - lpha_{s,k}^{Eng} \right\ _2^2 - arepsilon_lpha \le 0$	(18)
$g1: \left\ \alpha_s - \alpha_{s,k}^{Eng}\right\ _2^2 - \varepsilon_\alpha \le 0$	(18

$$g2: \left\| r_{1,s} - r_{1,s,k}^{Eng} \right\|_{2}^{2} - \varepsilon_{r_{1}} \le 0$$
(19)

$$g3: \left\| r_{2s} - r_{2s,k}^{Eng} \right\|_{2}^{2} - \varepsilon_{r_{2}} \le 0$$
(20)

967 Here,

968		
969	$\alpha_s$	Vane angle linking variable at the component sharing level.
970	$\alpha_{sk}^{Eng}$	Value of vane angle linking variable response of engineering design model for product
971	5,1	<i>k</i> .
972	$r_{1,s,k}$	Inner tube radius $(r_1)$ linking variable at the component sharing level.
973	$r_{1,s,k}^{Eng}$	Value of inner tube radius $(r_1)$ linking variable response of engineering design model
974	1,5,8	for product <i>k</i> .
975	$r_{2,s,k}$	Outer tube radius $(r_2)$ linking variable at the component sharing level.
976	$r_{2sk}^{Eng}$	Value of outer tube radius $(r_2)$ linking variable response of engineering design model
977	2,3,8	for product k.
978	Ea	Deviation tolerance variable between vane angle linking variable that is minimized in

 $\frac{978}{8}$   $\varepsilon_{\alpha}$  Deviation tolerance variable between vane angle linking variable that is minimized in the objective function.

980 $\varepsilon_{r1}$ Deviation tolerance variable between inner radius linking variable that is minimized in<br/>the objective function.

982 $\varepsilon_{r2}$ Deviation tolerance variable between outer radius linking variable that is minimized in<br/>the objective function.

To minimize overall product portfolio costs, the number of unique vane section designs will be minimized by sharing this component with products that can attain a feasible design solution given this added objective. Equation (13) is, therefore, reformulated to reflect the candidate product families and also the shared vane components among each of these products within a given product family (represented as linking variables).

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Lower level: Product family optimization

993 Minimize:

$$+ \|r_{1s} - r_{1s,k}^{Link}\|_{2}^{2} + \|r_{2s} - r_{2s,k}^{Link}\|_{2}^{2}$$
(21)

 $F(x)_{Architecture_{(k)}} = w'_{\zeta} \left\| \xi_{k}^{C_{j}} - \xi_{k}^{Eng} \right\|_{2}^{2} + w'_{AF} \left\| AF_{k}^{C_{j}} - AF_{k}^{Eng} \right\|_{2}^{2} + Cost_{k} + \left\| \alpha_{s,i} - \alpha_{s,k}^{Link} \right\|_{2}^{2}$ 

1000 Subject to: Constraints as defined in Equations (14), (15) and (16).

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\*Optimal results attained using Matlab<sup>®</sup> and Tomlab<sup>®</sup> to solve the mixed integer nonlinear programming problem (Griffiths 2005, Holmstrom *et al.* 2006).

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#### 1051 **5. Results and discussion**

### 1053 5.1. Aerodynamic particle separator optimization results

Given the product design targets from the data mining X-means clustering step, the aerodynamic particle separator model first attempts to identify feasible design solutions for the efficiency ( $\zeta^{Cj}$ ), flow area ( $AF^{Cj}$ ) targets and given physical and environmental ( $T_{air}$ ,  $P_{air}$ , etc.) parameters for each unique cluster centroid ( $C_j$ ). The aerodynamic particle separator solutions in Table 5 reveal that a total of five unique products can be designed for the initial five cluster centroids targets generated by the X-means clustering with a total product portfolio cost of \$173,910.

If Step 1 of the product family design methodology is successful, engineers can further inves-1061 tigate the potential costs savings (Steps 2 and 3) that may be realized due to component sharing. 1062 The X-means clustering technique performed during Step 2 reveals that out of the five unique 1063 aerodynamic particle separator solutions, products 1 and 5 form a feasible unique product family 1064 cluster, products 2 and 3 another and finally product 4 cannot be shared with any other product 1065 and, therefore, reverts back to the original solution from Step 1. The cost of the injection mould 1066 manufacturing process presents an opportunity for the initial product portfolio of five unique 1067 products to be redesigned. The vane section of the product which is made through the injection 1068 moulding process is shared among similar products existing in the original portfolio. In this case 1069 study, the decision to share the vane angle is known as a priori due to the high cost of designing 1070 each individual injection mould for the vane. Step 3 of the product family design methodology 1071 employs the X-means clustering algorithm to identify products that have similar vane design 1072 solutions. The decision to share the vane angle is an attempt to minimize the overall costs of the 1073 enterprise product portfolio by minimizing the number of unique vane sections needed for the five 1074 aerodynamic particle separators. Products successfully sharing a vane section will be considered 1075 a unique product family and each product existing in this product family, is defined as a variant. 1076 However, it must be noted that the cost savings benefits of component sharing using the product 1077 family approach to design may be offset by the decrease in the performance capabilities attain-1078 able by the newly designed product variants. This trade-off scenario will, therefore, be based on 1079 how much cost savings can be realized through component sharing and how much performance 1080 deviation can be accommodated by the customer. 1081

The results in Table 6 reveal that sharing products 1 and 5, 2 and 3 (with product 4 being a 1082 separate unique design), reduces the total product portfolio cost to \$163,150; a total savings of 1083 approximately \$10,760 for this product portfolio design scenario. However, it can be observed 1084 that the efficiency of product 2 decreases from 85.99% with the individual optimization model 1085 solution (Table 5) to 85.84% with the component sharing product family model solution (Table 6). 1086 The level of allowable performance deviation will be dependent on customer expectations and the 1087 level of competition within the market space. Although a feasible design may not always exist for 1088 every sharing scenario (for example sharing a single vane component for each of the five products 1089 returned an infeasible solution), the benefits of investigating sharing strategies through the X-1090 means clustering recommendations may prove beneficial as can be seen from the results in Table 6. 1091

#### 1093 1094 **6. Conclusion**

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1096 In this work, a comprehensive product family design methodology is presented that integrates 1097 realistic product operation data with the engineering design of complex products such as the 1098 aerodynamic particle separator. The data mining RELIEFF algorithm is employed to determine 1099 the weights of each attribute. This information is then incorporated into the data mining X-means 1100 clustering algorithm in order to generate the number of clusters along with the cluster centroids

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that are inherent to the data itself. The results of the data mining clustering technique aid in 1101 determining the number of unique products to design for a group of highly diverse customers. 1102 1103 With this clustering information, a product architecture can be designed that takes into account specific customer product functionality needs that are represented in a large data set. Further cost 1104 1105 savings can be realized through a component sharing strategy that is achieved in this work by 1106 once again employing the X-means clustering technique to identify similar design solutions. The 1107 hope is to expand on the concepts presented in this work by enabling the feasibility of the product 1108 architecture optimization step to influence the generation of X-means cluster centroids. That is, local objective functions may be highly sensitive to certain local design variables which can be 1109 1110 taken into account during the X-means clustering step. 1111

#### 1112

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#### 1119 Note

### 1120

1. The initial version presented at the 12th AIAA/ISSMO Multidisciplinary Analysis and Optimization Conference, 1121 Victoria, British Columbia, Canada. 1122

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